New Circumstellar Magnetic Field Diagnostics

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Abstract. We discuss the potential of scattering diagnostics for magnetic field studies in circumstellar material. We briefly mention related instrumentation development efforts.

1. Introduction

Few magnetic diagnostics are useful in the circumstellar environment. Table 1 lists the common magnetic diagnostics, the component of the field they are sensitive to, whether they measure field strength or geometry, the wavelengths used and field magnitudes measurable, additional requirements for their use, and their astrophysical application. In this paper we discuss the last two, the “scattering” diagnostics, which have heretofore been applied only to the Sun.

2. Scattering magnetic diagnostics

The scattering diagnostics are based on the polarization from atomic fluorescent scattering. Here we summarize the physics behind the effect.

2.1. Atomic scattering

The theory of polarization from atomic scattering is summarized in Ignace, Nordsieck & Cassinelli (1997) and treated in detail in Stenflo (1994). To start, we assume thermodynamic equilibrium and the absence of a magnetic field. In this case any one fluorescent scattering process (lower state to upper state to some possibly different lower state) can be treated as the sum of some fraction $E_1$ of polarized dipole scattering and the fraction $(1 - E_1)$ of unpolarized isotropic scattering. For illumination by an unpolarized beam, the degree of linear polarization $p$ of the scattered beam (our observable) as a function of scattering angle $\theta$ is $p(\theta) = \frac{3}{4}E_1 \sin^2 \theta/(1 - \frac{1}{4}E_1 + \frac{3}{4}E_1 \cos^2 \theta)$. This “dipole-like” scattering has a polarization with a maximum at 90° scattering which is proportional to $E_1$. For an “unaligned” atom (all ground magnetic substates equally populated) the “polarizability” $E_1$ may easily be calculated from formulae in Stenflo which depend only on the angular momentum $J$ of the atomic levels. $E_1$ is in the range $-1 < E_1 < 1$, where positive denotes polarization perpendicular to the plane of scattering, and negative polarization is parallel to the plane. Basically, the polarization properties of an isolated atom are summarized by a single known parameter, $E_1$. 

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Table 1. Magnetic diagnostics.

<table>
<thead>
<tr>
<th>Method</th>
<th>Comp</th>
<th>Strength</th>
<th>$\lambda$'s</th>
<th>Field</th>
<th>Requires</th>
<th>Useful for</th>
</tr>
</thead>
<tbody>
<tr>
<td>Faraday Rotation</td>
<td>Long</td>
<td>$N_e B \ell \lambda^2$</td>
<td>rad</td>
<td>$&lt; \mu G$</td>
<td>Bkg pol</td>
<td>diffuse ISM</td>
</tr>
<tr>
<td>Gyrocyclotron Rad'n</td>
<td>Long</td>
<td>rad</td>
<td>0.1-10kG</td>
<td>Ionized gas</td>
<td>Source</td>
<td>ISM coronae</td>
</tr>
<tr>
<td>Synchrotron Polarization</td>
<td>Trans</td>
<td>rad</td>
<td>$\mu G$</td>
<td>Relativistic</td>
<td>electrons</td>
<td>diffuse ISM</td>
</tr>
<tr>
<td>IR Dust Emission</td>
<td>Trans</td>
<td>vis</td>
<td>$\mu G$</td>
<td>heated dust</td>
<td>ISM</td>
<td>mol. clouds</td>
</tr>
<tr>
<td>Interstellar Polarization</td>
<td>Trans</td>
<td>UV-NIR</td>
<td>$\mu G$</td>
<td>Dust; Bkg</td>
<td>ISM, source</td>
<td>clouds</td>
</tr>
<tr>
<td>Zeeman Effect</td>
<td>Long</td>
<td>$g_L \lambda B$</td>
<td>vis</td>
<td>$\mu G$</td>
<td>narrow line</td>
<td>ISM, stars</td>
</tr>
<tr>
<td>Hanle Effect</td>
<td>Nirm (line)</td>
<td>UV</td>
<td>$\mu G$</td>
<td>Atom scat</td>
<td>stars</td>
<td>winds</td>
</tr>
<tr>
<td>Magnetic Realignment</td>
<td>Nirm (illum)</td>
<td>UV</td>
<td>$&lt; \mu G$</td>
<td>Atom scat</td>
<td>circums*</td>
<td>material</td>
</tr>
</tbody>
</table>

The strongest scattering lines in astronomy, and the easiest to understand spectroscopically, are the "alkali-like doublet" resonance lines, which arise from the ground state of ions with a single electron above a closed shell (NaI, CaII, NV, etc.). In this paper we will concentrate on these lines, giving specific examples for sodium. For the alkali-like doublets, it turns out that the red line is always unpolarized, $E_1 = 0$, while the blue line is positively polarized. This is a unique signature for line scattering: an unpolarized red line indicates that there are no other processes, like electron scattering of line emission, contaminating the line scattering polarization. For the blue line, in those atoms without hyperfine structure (OVII, CIV, SiVI, MgII, and CaII), $E_1 = 0.5$, a very high polarizability, producing a strong polarimetric signal.

All this is of interest because the observed polarization law $p(\theta)$ can be modified by its environment, namely by the magnetic field, and/or by the presence of a strong illuminating flux. As a result, we can in principle observe $p(\theta)$ and deduce the environment of the atom. There are three potential complications in the analysis. The first is optical depth: This is relevant for applications of scattering diagnostics to the solar atmosphere, but not for many circumstellar applications. We shall for now assume $\tau \ll 1$, so that the observed polarization is just that of the Doppler core from isolated atoms. A second complication is a non-point illuminator: Again, while this is a problem in the solar photosphere, it is not a serious problem in the optically thin outer parts of most stellar winds. Third, the most serious complication is that we measure only the polarization $P$ and we need an independent estimate of the scattering angle $\theta$. In the best case we can observe the polarization at a known scattering angle (e.g. comets). More usually, the scattering angle must be inferred from other information. The method that we advocate here is the use of velocity information through observation of the polarimetric line profile. For instance, for a resolved purely expanding wind (e.g., a planetary nebula), along a particular line of sight the
Doppler-shifted wavelength of the line is uniquely related to the position along the line of sight, and thus to the scattering angle. For an unresolved stellar wind, the different lines of sight may be dissected using a model of the radial dependence of the wind (Cassinelli, Nordsieck, & Ignace, this volume).

2.2. Hanle effect

The Hanle Effect occurs for fields strong enough that the Larmor frequency $\omega_L$ is of the same order or greater than the inverse lifetime $A_{ul}$ of the upper level of the atom. Classically, the Hanle effect can be treated as a dipole radiator where precession occurs while the atom is re-emitting the line radiation. The presence of a field changes both the degree and angle of the line polarization. The Hanle effect is significant for fields greater than the “Hanle field” $B_H$, $B_H = A_{ul} e g_L/m_e c = 5 \text{ Gauss} \times (A_{ul}/10^8)$, where $g_L$ is the Lande factor. The Hanle Effect results in a polarization vs. scattering angle law that is no longer “dipole-like”, depending not only on the polarizability $E_1$ but also on $B$ and on the direction between the magnetic field and the illuminating radiation. It applies to any fluorescent transition for which $E_1 \neq 0$. The polarization law varies measurably with field strength for small fields, and then becomes “saturated” (gives angle information only) when $B \gg B_H$. Unlike the Zeeman Effect, the Hanle Effect affects the integrated line, so Doppler broadening does not destroy it. This makes it ideal in a dynamic circumstellar environment.

Figure 1 shows the Hanle field for the doublet lines of some of the most abundant alkali-like ions. $B_H$ rises from 3 G for lines in the visible, to 60 G in the far ultraviolet. These are quite small fields compared to those detected by the Zeeman Effect, and they are very interesting fields for inner stellar winds. The Hanle Effect has been applied in the visible to the Sun, for instance on the sodium D lines. For stars hotter than the Sun, sodium is ionized and ions of higher ionization potential (right-hand scale in Fig. 1) with lines in the UV and

Figure 1. Left scale. Hanle Field for the alkali-like doublets, vs wavelength of the line: square: hydrogen-like; diamonds: lithium-like; triangles: sodium-like; circle: potassium-like. Filled: alignable due to hyperfine structure. Right scale (crosses): Ionization potential in eV.
FUV, are more appropriate. These lines are quite strong in hot stars and are in fact among those responsible for driving their winds.

2.3. Hyperfine structure

The open symbols (CIV, OVI, MgII, SiIV, and CaII) in Fig. 1 are simple doublets; the ground state is \(^2S_{1/2}\) and the upper states are \(^2P_{1/2}\) and \(^2P_{3/2}\). The line of longer wavelength ("L1") always has \(E_1 = 0\), so is unpolarized, and the L2 line always has \(E_1 = 0.5\). In an interesting complication, the filled symbols in Fig. 1, (NV, NaI, AlIII, PV, and KI), represent ions with nonzero nuclear spin, therefore possessing hyperfine structure. For these, the (nondegenerate) hyperfine lines must be treated individually, using total angular momentum \(F\) instead of \(J\). It can be shown that the net polarizability for the L1 line (now a hyperfine multiplet) is still zero, while for L2 it is some nonzero number that depends on the nuclear spin and on which hyperfine levels are nondegenerate. For example, for \(^{23}\)Na (the common isotope of sodium), the nuclear spin is \(\frac{3}{2}\), so that the ground state is split into two sublevels and the upper levels are split into two and four sublevels. The sodium nuclear moment is rather large, so these hyperfine levels are all nondegenerate. The net polarizability of the D1 and D2 lines is then a weighted mean of the hyperfine components. For the Na D1 line one finds \(E_1 = 0\), and for the D2 line, \(E_1 = 0.135\).

The presence of hyperfine structure has two effects on the alkali doublets. It does reduce the polarizability of the L2 line, and thus the magnitude of the Hanle Effect. But more important, it makes the atom susceptible to alignment effects which are sensitive to magnetic field in another way:

2.4. Fluorescent alignment

Any atomic level with at least three fine or hyperfine levels (\(J \text{ or } F \geq 1\)) may be "aligned". In the framework of quantum mechanics, this means that the \(M\) substates are not uniformly populated, and classically it means that in an ensemble of atoms the angular momenta are not isotropically distributed. A familiar form of atomic alignment is "optical pumping" through fluorescence. This can be understood on the basis of quantum mechanical selection rules between the \(M\) substates of the lower and upper levels. It will persist as long as the photon excitation rate \(R_F\) is greater than the collision rate \(R_C\), a situation which holds for many dilute circumstellar envelopes near bright stars. For the alkali-like doublets, this occurs only for those atoms with hyperfine structure, where \(F \geq 1\).

Atomic fluorescent alignment has been studied extensively in the laboratory (see Happer 1972). Laboratory studies of sodium alignment, pioneered by Brosel, Kastler and Winter (1952) and Hawkins (1954), provide a good benchmark.

The importance of fluorescent alignment to this paper is that it (and its modification by a magnetic field), produces an observable change in the atomic polarizability. For the alignable alkali doublets, the magnitude of the effect depends on the amount of pumping and on the level structure, which depends on the nuclear spin. The effect of fluorescent alignment may be evaluated by a standard statistical equilibrium calculation of the magnetic sublevel population distribution, where the only transitions are fluorescent transitions illuminated from a single direction. Figure 2 shows the population of the \(M\) states for the alignable alkali doublets for complete fluorescent alignment \((R_F \gg R_C)\), with
Figure 2. Relative M state ground level populations for fluorescently aligned alkali-like ions. Filled, lower hyperfine level; open, upper hyperfine level.

Figure 3. 3a (left), change in polarizability due to fluorescent alignment, vs unaligned polarizability for $L_2$ line of alkali-like doublets. 3b (right), polarizability as a function of angle between illumination vector and magnetic field for saturated magnetic realignment of Na D.

nuclear spins $I = \frac{1}{2}$ (PV), 1 (NV), $\frac{3}{2}$ (NaI, KI) and $\frac{5}{2}$ (AlIII). The upper hyperfine level (highest $F$) is overpopulated, with the states of highest absolute value angular momentum most overpopulated. For example, for NaI, $|M_F| = 2$ is overpopulated by 60%, and the polarizability of the $D_2$ line goes from 0.135 to 0.217. Thus aligned Na atoms give a substantially higher polarizability than unaligned ones, by a factor of 1.6, which is easily observed.

Figure 3a shows a summary for all the alkali doublets. The vertical axis shows the change in polarizability for completely aligned atoms, while the horizontal axis shows the polarizability for unaligned atoms.

2.5. Magnetic realignment

Fluorescent alignment is interesting to us because it can be altered by a magnetic field. The magnetic field mixes the $M$ sublevels of the atoms, but only perpendicular to the field. Thus if the Larmor precession rate $\omega_L$ exceeds the rate of photon arrival $R_P$, the atoms are “realigned” to the magnetic field. This effect, “magnetic realignment”, is observable through a change in the polariz-
ability $E_1$, which now depends on ratio of the Larmor frequency to the photon arrival rate, and on the angle of the magnetic field to the photon illumination direction. Recently, the importance of atomic fluorescent alignment and magnetic realignment for optical transitions has been realized by solar researchers (see Trujillo Bueno & Landi Degl'Innocenti 1997).

For circumstellar envelopes, magnetic realignment is a potentially powerful magnetic diagnostic. Like the Hanle Effect, it depends on field strength for small fields and becomes “saturated” (gives angle information only) for fields where $\omega_L \gg R_F$. It affects the integrated line, so broadening does not destroy it. Unlike the Hanle Effect, it is sensitive to very small fields. Defining a “realignment” field $B_A$, the field for which $\omega_L \sim R_F$, we find for sodium $B_A = (\alpha F_\nu / h\nu)(e g_L / m_e c) = 0.3 \mu\text{Gauss} \times (L_\nu / L_\nu(\text{sun}))/ (R_{\text{AU}})^2$, where $\alpha$ is the line cross-section, $F_\nu$ and $L_\nu$ is the illuminating flux and luminosity at the line frequency, and $R_{\text{AU}}$ is the distance in AU from the star. Realignment should be dominant in the outer circumstellar environment.

As an example, we have calculated the effect of saturated magnetic realignment on NaI in the limit of very small fields ($B_A \ll B < B_H$). For a field oriented at angle $\phi$ to the illuminating beam, the effective $M$ state population may be calculated using a procedure given in Hawkins (1954): the effective $M$ state population of the ensemble is evaluated by taking a time average of the frequency of occupation of each $M$ state over the period between the arrival of one photon and the next. Given the new $M$ state population, $E_1(\phi)$ for the Na D lines is evaluated. Once more, for D1 the polarizability remains 0, while for D2 it is intermediate between the unaligned and aligned cases. Figure 3b shows the results for the net polarization of the D2 line as a function of magnetic field angle. The observed polarization is insensitive to magnetic field along the illumination axis, but is quite sensitive for nonzero angles up to 45°.

### 2.6. A diagnostic diagram

The ultimate result for the scattering diagnostics is that $p(\theta)$ for an ion depends on the magnetic field through the effect of realignment on $E_1$, and/or through the Hanle Effect modification of the form of $p(\theta)$. In the circumstellar context, the Hanle Effect is appropriate for moderate fields in usually unresolved inner winds, while magnetic realignment becomes interesting in outer nebulae (possibly resolved) where it is sensitive to very small fields. The Zeeman Effect, on the other hand, is useful in the large fields in or near stellar photospheres.

Figure 4 summarizes these magnetic diagnostics. It applies specifically to Na D, but should be qualitatively correct for the other hyperfine split alkali doublets (KI, NV). The vertical axis is the illuminating flux, normalized to the flux at the surface of the Sun. In a particular envelope, this depends just on the distance from the star. Approximate flux levels for the pilot observations proposed below are shown. For the spinless alkali-like ions (CaII, CIV, SiIV), only the Hanle Effect will apply, so that the vertical axis and all the alignment-dependent lines would not appear, although the Hanle Effect regimes would still appear. Both magnetic realignment and the Hanle Effect have regimes (light gray) where both the strength and angle of the magnetic field may be inferred, and “saturated” regimes (dark gray) where the angle of the field may be deduced and a lower limit may be placed on the strength.
3. Instruments/Investigations

The scattering diagnostics are still young, so it is not surprising that they have not been applied beyond the Sun. Lack of appropriate instrumentation is a serious barrier. First, one encounters the limited spectral resolution of most linear polarization spectropolarimeters. These diagnostics benefit from \( R = \lambda/\Delta \lambda > 5000 \), required to resolve lines and to avoid unpolarized continuum contamination and noise. Second, because of signal/noise requirements, one needs larger telescopes and higher efficiency than are usually available. Third, some of the diagnostics are better applied in the vacuum ultraviolet, where polarimetry is still in its infancy. And finally, for the realignment diagnostic, observations of faint diffuse lines require unusually high etendue, that is, high spectral resolution on diffuse targets. Below we present two pilot observations together with instrumentation which is being developed to perform them.

3.1. Ultraviolet spectropolarimetry

Application of the Hanle Effect to hot star winds is an obvious direction to pursue, since the scattering lines are so prominent and the stars so bright, and the magnetic fields which could be detected only in this way would be very important in the dynamics of the wind. At the University of Wisconsin we have been developing the Far Ultraviolet SpectroPolarimeter (FUSP) to explore this type of observation, among others. A simulated observation of the O star ζ Ori with FUSP is discussed in Cassinelli et al. (these proceedings).
Figure 5. Simulated polarization profile for a Na D_{2} line of sight through a Planetary Nebula. Left: cartoon showing relation between scattering angle and Doppler velocity. Right: polarimetric profile under various assumptions for the magnetic field.

FUSP is a sounding rocket payload designed to obtain the first spectropolarimetry in the far ultraviolet (Nordsieck 1999). It will cover wavelengths 1050 - 1500 Å with a resolution $R = 1800 \ (0.5 \ Å; 180 \ km/sec)$. The telescope aperture is 50cm and the spectropolarimeter is at the prime focus. Polarimetric modulation is provided by a rotating halfwave plate of stressed lithium fluoride. The polarization analyzer is a 12 mm square artificial diamond Brewster angle mirror. The spectrometer uses a spherical aberration-corrected holographic grating. A two-stage rocket will carry the payload to an apogee of 400 km, giving a total usable science time of 400 sec. The scheduled first launch is in 2002, with a “Hanle Effect” launch targeting ζ Ori and the rapid rotator ζ Per in 2003. FUSP is intended to provide proof of principle for later development of a small satellite for FUV spectropolarimetry.

3.2. High resolution spectropolarimetric imaging

Magnetic realignment appears to be most interesting for the outer parts of circumstellar envelopes, where its sensitivity to very small fields provides a unique capability. We are pursuing as pilot projects observations of resolved nebulae where the scattering angle is most easily deduced. There are a number of targets with known Na D scattering nebulae, including comets, M supergiant stars, and Planetary Nebulae, which are then observable in the visible, albeit with large telescopes due to the faintness of the line emission.

An exciting prospect is the detection of magnetic fields in Planetary Nebulae. The presence of a field has been suggested by dynamic models of the bipolar geometry of the nebulae. Field geometries have been suggested based on models of the evolution of the field in AGB stars (Thomas et al., this volume). Fluorescent Na D has been seen so far in 5 Planetary Nebulae by Dinerstein, Sneden & Uglum (1995). The sodium is apparently in the neutral shell around the nebulae. At this distance from the central illuminator, the realignment field is less than 1 μG, so that any dynamically important field should be easily detected. Interpretation of the results is made relatively straightforward by the simple 30 km/s spherical expansion of the nebula (Fig. 5). With a resolution of $R > 10,000$ one can resolve the expansion profile. Each point along the line of sight then corresponds to a unique scattering angle and a unique Doppler
velocity, so that there is a one-to-one correspondence between the position in the profile and the scattering angle. The figure shows the expected signal for unaligned atoms (very unlikely), aligned with no magnetic field, and a saturated magnetic field 30 degrees from the radius vector to the star. With a map of the polarimetric profile one can in principle obtain two components of the field geometry in three dimensions. Observations like this will require a large telescope, since the Na D emission strength is only of order 50 Rayleighs (1 Rayleigh = \(10^8\) photons/sec/4\(\pi\) sr) and the nebulae subtend less than 0.5 arcmin.

Such an instrument will become available soon: The University of Wisconsin is constructing a high-throughput medium resolution imaging spectropolarimeter for the Southern African Large Telescope (SALT). SALT will be a 10m telescope based on the Hobby-Eberly Telescope (HET) segmented mirror design. The Prime Focus Imaging Spectropolarimeter will operate with a simultaneous dual visible/NIR beam over 3200 Å–1.7 \(\mu\)m; the visible beam will be commissioned first, in 2004. Slitmask and long-slit spectropolarimetry will be available over an 8 arcmin field of view. The polarimetric modulator will be a superachromatic waveplate, and the analyzer will be a calcite beamsplitter. Spectropolarimetry will be available in two modes, grating and Fabry-Perot. The grating spectropolarimeter uses Volume Phase Holographic ("VPH") gratings for very high efficiency. Resolution will be \(R = 800 - 6500\) with an 0.9 arcsec slit (median seeing) and 12,000 with a 0.5 arcsec slit. Dual etalon Fabry-Perot spectropolarimetry will also be available with resolutions of 2500 and 13,000. For the Na D Planetary Nebula pilot project described above, we estimate that a single 1 hour Fabry-Perot observation will obtain a Na D polarimetric "data-cube" with 1% polarimetric error/resolution element over the entire nebula.

4. Summary

We find that for the circumstellar environment, the scattering magnetic field diagnostics may be the most appropriate. The Hanle Effect used on FUV resonance lines may be valuable for determining the existence of dynamically important fields (0.1–300 G) in OB star winds. Magnetic realignment is a promising magnetic diagnostic of very small fields (\(\sim 1 \mu G\)) in the outer circumstellar environment. Instrumentation in development will allow these methods to be tested.

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References

Happer, W. 1972, Rev. Mod. Phys., 44, 169
Discussion

LANDI DEGL'INNOCENTI: Could you please explain in more detail what is the difference between the Hanle Effect and the phenomenon that you call “re-alignment”?

STENFLO: There is some confusion about the terminology used. As I understand it, when you talk about magnetic realignment, what you mean is the magnetic modification (Hanle Effect) of the ground-state atomic polarization.

NORDSIECK: We have been struggling, as newcomers to the scattering diagnostics, to apply the experience of solar astronomers to the rather different circumstellar environment. I think some of the difficulty is terminology, but that there may be more interesting insights from the different regimes. I understand that solar astronomers use the “Hanle Effect” as a blanket term to cover all effects that involve modification of the polarization through the “realignment” of the states of both the upper and lower levels of a transition. Solar astronomers deal with relatively large magnetic fields that are comparable with the Hanle field, so that there is significant realignment taking place during the scattering process. I would agree that in this case it is the same effect for both upper and lower states. Perhaps we could agree to call this the “classical” Hanle Effect. We, on the other hand, have been exploring the magnetic realignment of the lower state in a very different regime where the field is much less than the Hanle Field. This seems to me to be qualitatively different. Here, all of the precession of $M$ states occurs before the scattering process, and because of this, quantum mechanics requires us to sum results incoherently over an ensemble of atoms in different $M$ states. I think this difference explains why in the classical Hanle Effect (field comparable to the Hanle Field), the polarization phase function becomes non-dipole, with position angle rotations, etc., while in what I call magnetic realignment (very small field), the polarization remains dipole, with a change only to the polarizability.

WADE: Your illustrative calculations regarding the Hanle Effect in ζ Ori were very interesting. You took the envelope geometry to be spherical, and hence the emission is unpolarized in the absence of a magnetic field. In fact, ζ Ori, like most other stars, is rotating. Its envelope will therefore be somewhat oblate. How does this effect the calculations?

NORDSIECK: Yes, the model is very over-simplified. One other obvious problem is that a dipole field in a spherically expanding envelope is not dynamically consistent. We picked ζ Ori as a first example partly because it is not a fast rotator. It takes quite a lot of rotation before the wind becomes oblate enough to exhibit intrinsic polarization, so we think ignoring this is not a serious problem. That said, if there is sufficient flattening to cause polarization, it will occur for all scattering lines regardless of their Hanle Field, which should be separable from the Hanle signal, which is quite sensitive to Hanle Field. We do plan to look at a more rapidly rotating O star, ξ Per, to practise dealing with this complication.